

Numbers

Chapter 1

Class 1

• Sets →

$$21 \div 7 + 6 - 5 \times 3 = -6$$

• Ratios & Proportion

$$\underline{9 - 15} = -6$$

• Profits & Loss.

Round bracket $()$
Small bracket $()$

$$\underline{12} - \left[\underline{6 \div 3} + \left\{ 8 \div 2 \left(\underline{8-6} \right) \right\} \right]$$

$[]$ → Square bracket
→ Big bracket.

$$\Rightarrow 12 - \left[2 + \left\{ 8 \div \underline{2 \times 2} \right\} \right]$$

$\{ \}$ → curly bracket
→ Braces

$$\Rightarrow 12 - [2 + 8]$$

$$\Rightarrow 12 - 10$$

$$\Rightarrow 2 =$$

Prime nos. less than 20. 48,

2, 3, 5, 7, 11, 13, 17, 19

LCM (12, 16)

$$\text{LCM (48, 72)} = \underline{2 \times 2} \times \underline{2 \times 2} \times 3 \times 3 = \underline{\underline{144}}$$

$$\begin{array}{r} 16 \\ \times 9 \\ \hline 144 \end{array}$$

LCM(96, 108, 120)

short-division method

2 | 96, 108, 120 ✓

→ $2^5 \times 3^3 \times 5^1$

⇒ $32 \times 27 \times 5$

⇒ 4320

HCF (60, 72)

| | |
|---|------------|
| 2 | 60, 72 |
| 2 | 30, 36 |
| 3 | 15, 18 |
| | <u>5 6</u> |

$$\begin{aligned} \text{HCF} &= 2 \times 2 \times 3 \\ &= 12 \end{aligned}$$

$$\text{HCF}(56, 84, 154) = 2 \times 7 = 14$$

| | |
|---|-------------|
| 2 | 56, 84, 154 |
| 7 | 28, 42, 77 |
| | 4, 6, 11 |

Fractions:

$$\frac{7}{5} \div \frac{28}{40}$$

$$\frac{7}{5} + \frac{2}{15}$$

$$\frac{7}{5} + \frac{2}{5}$$

$$\frac{7}{5} \times 3 = \frac{21}{15}$$

$$\frac{21}{15} + \frac{2}{15}$$

$$= \frac{7+2}{5} = \frac{9}{5}$$

$$\boxed{\frac{23}{15}}$$

$$\frac{\textcircled{7}}{5} \times \frac{\textcircled{15}}{14} = \frac{\overset{1}{\cancel{7}} \times \overset{3}{\textcircled{15}}}{\underset{1}{\textcircled{5}} \times \underset{2}{\cancel{14}}} = \frac{1 \times 3}{1 \times 2} = \frac{3}{2}$$

$$\frac{7}{5} \textcircled{\div} \frac{28}{40} = \frac{\textcircled{1} \cancel{7}}{\cancel{5}} \times \frac{\overset{82}{\cancel{40}}}{\underset{\cancel{4}}{\cancel{28}}} = \frac{1 \times 2}{1 \times 1}$$

$$= 2$$

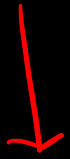
$$\underline{\text{HCF (135, 180)}}$$

$$\text{HCF (217, 305, 735)}$$

Class 2

201859

Place value and face value of 8 in the above no.!



$$8 \times 1000 = 8000$$



8

1 Mega $\rightarrow 10^6 \rightarrow 1000000$

1 Googol. $\rightarrow 10^{100}$

1 Googolplex $\rightarrow 10^{\text{googol}}$

$(10)^{10^{100}} \rightarrow 10^{(1000 \dots 100 \text{ zeros})}$

Search Engine: Google

↑
Misspelling of the word Googol

Integers

Natural Number :

↳ Counting number

eg. 1, 2, 3,, ∞

Whole Number :

Zero and natural numbers together are called whole number

eg. 0, 1, 2, 3, 4,, ∞

Integers

→ whole nos. + all negative number

eg $-\infty, \dots, -3, -2, -1, 0, 1, 2, 3, \dots, +\infty$

Integers are directed numbers

↓
Directional.

①

+45m

↓
45m above
sea level

-45m

↓ 45m below
sea level

↑ above sea level +ve number

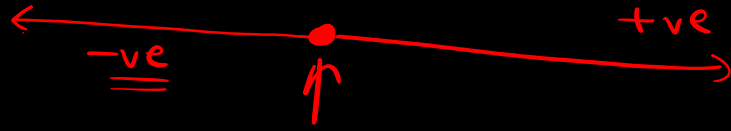
→ sea level

↓ below sea level is
represented using
-ve numbers

⑪ If the temperature above freezing point (0°C) is represented by +ve number, then the temp. below freezing point is represented by negative number (negative integer)

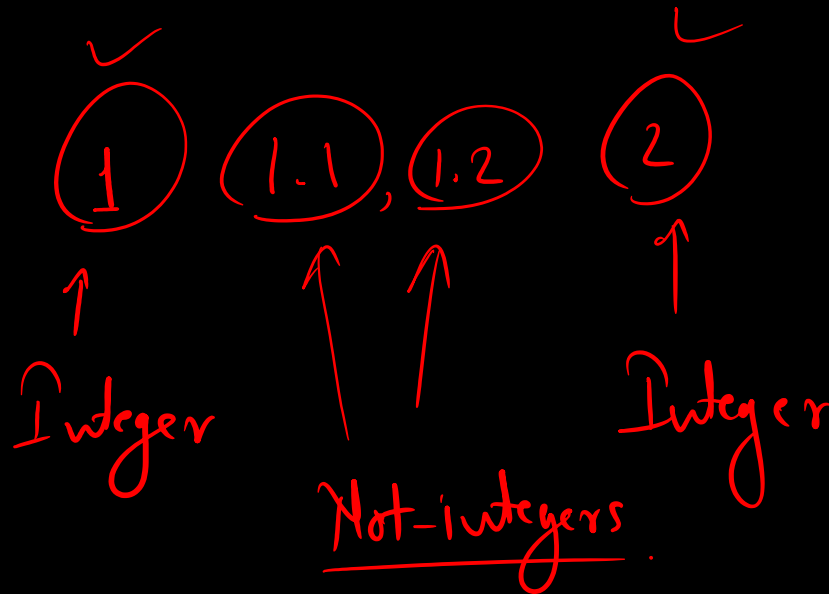
for ex. $\underline{13^{\circ}\text{C}}$ above freezing point \Rightarrow $+13^{\circ}\text{C}$
 13°C below freezing point \Rightarrow -13°C

Class 3

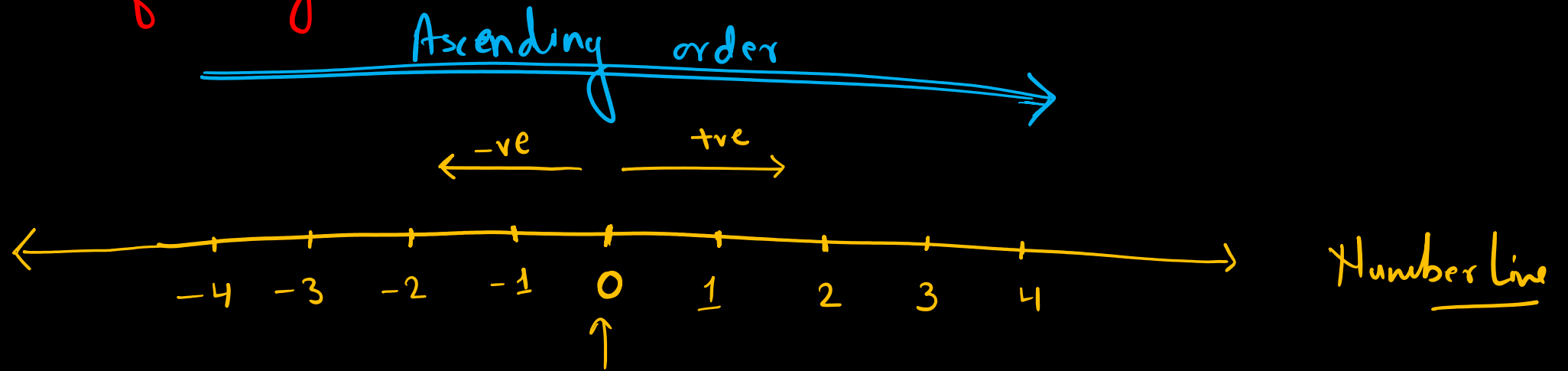


Reference Point

-3



Representation of Integers on number-line



Reference point / Starting point
(origin)

All non-negative integers : $[0, 1, 2, 3, \dots, \infty]$

All positive integers : $[1, 2, 3, 4, \dots, \infty]$

All non-positive integers : $[0, -1, -2, -3, \dots, \infty]$

Addition and Subtraction of Integers

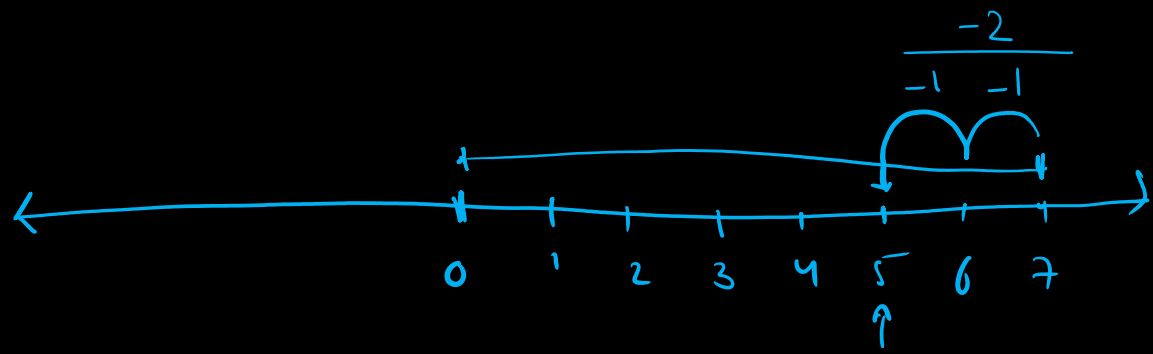
$$+7 = 7$$

① Add two positive integers.

$$(+2) + (+5) = 2 + 5 = 7$$

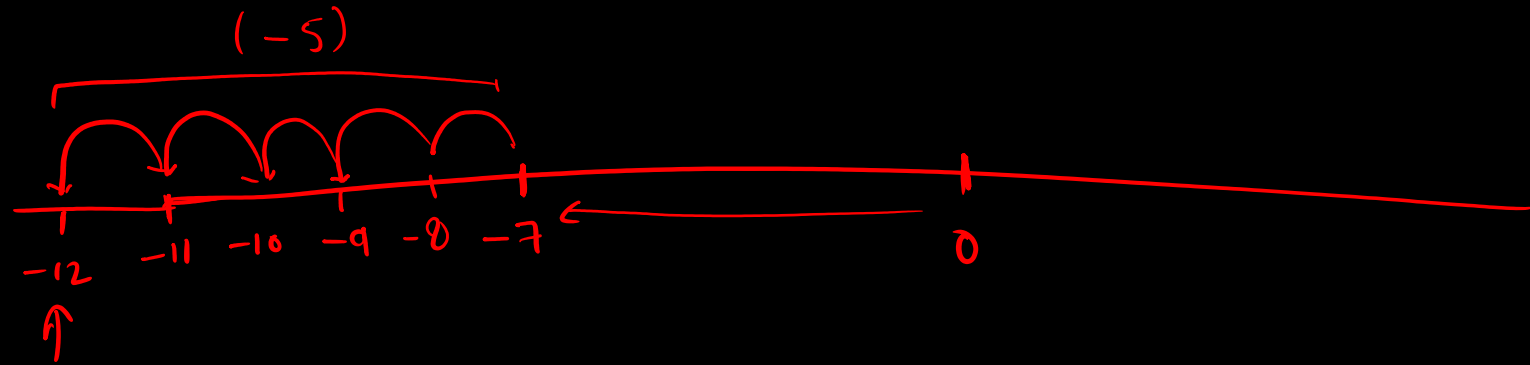
② Add a negative integer to a positive integer.

$$(+7) + \underbrace{(-2)}_{\ominus} = 7 - 2 = 5$$



$$(ii) \quad 7 + (-9) = 7 \ominus 9 \\ = -2$$

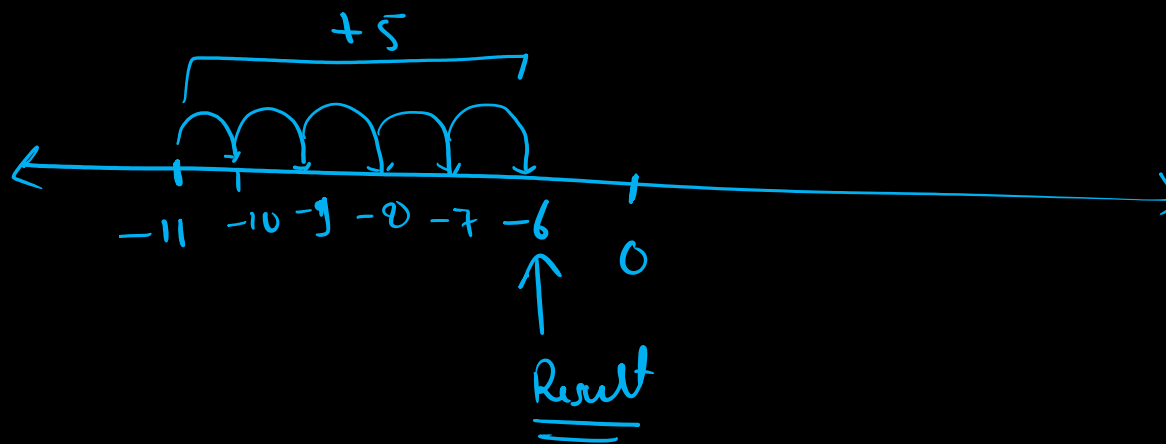
$$(iii) \quad (-7) + (-5) = \underline{-7 - 5} = \underline{\underline{-12}}$$



$$(iv) \quad (-15) + (-19) = -15 - 19 \\ = -34 \quad \left. \vphantom{(-15) + (-19)} \right\} \begin{array}{l} \text{Add the nos. and put} \\ \text{-ve sign.} \end{array}$$

$$\textcircled{v} \quad \underline{\underline{-11}} + 5 = \underline{\underline{-6}}$$

$$\begin{array}{r} 11 \\ -5 \\ \hline 6 \end{array}$$



$$\Rightarrow \quad -13 + 2 = -11$$

$$\Rightarrow \quad \begin{array}{r} -17 \\ \uparrow \end{array} + \begin{array}{r} 25 \\ \uparrow \end{array} = +8$$
$$= 8$$

$$\textcircled{\text{vi}} \quad -6 - (-11) = -6 + 11 = 5$$

$$7 - (-10) = 7 + 10 = 17$$

$$-12 - (19) = -\underline{\underline{31}}$$

$$\underline{\underline{-12}} - (-19) = -12 + 19 = \underline{\underline{7}}$$

Class 4

$$\underline{\underline{1.}} \quad 12 + \underline{(-19)} - \underline{(-7)}$$

$$\Rightarrow 12 - 19 + 7$$

$$\Rightarrow -7 + 7$$

$$\Rightarrow 0$$

$$\underline{\underline{-30 - 18}}$$

$$\underline{-48 - 11}$$

$$\Rightarrow \underline{\underline{-59}}$$

$$\underline{\underline{2.}} \quad \underline{\underline{-30}} + 19 + 23 - \underline{\underline{18}} + \underline{7} - \underline{\underline{11}} + \underline{3}$$

$$\Rightarrow \underbrace{19 + 23 + 7 + 3} - \underbrace{30 - 18 - 11}$$

$$\Rightarrow \underline{\underline{52 - 59}}$$

$$\Rightarrow -7$$

$$\underline{\underline{3.}} \quad 86 - 72 + 33 - 48 + (-14) - (-26)$$

$$\Rightarrow 86 + 33 + 26 \quad \underbrace{-72 - 48 - 14}$$

$$\Rightarrow \underbrace{145 - 134}$$

$$\Rightarrow \underline{\underline{11}}$$

$$\underbrace{-72 - 48 - 14}$$

Multiplication of integers

Ex. $\underline{2} \times \underline{6} = 12$

 ↓ ↓ ↓

 +ve +ve +ve

⇒ $2 \times (-6) = \underline{\underline{-12}}$

 ↓ ↓ ↓

 +ve -ve -ve

Important Box ✓

| | | | | |
|---|---|---|---|---|
| ⊕ | × | ⊕ | = | ⊕ |
| ⊕ | × | ⊖ | = | ⊖ |
| ⊖ | × | ⊕ | = | ⊖ |
| ⊖ | × | ⊖ | = | ⊕ |

positive (+ve)
negative (-ve)

$$\textcircled{i} \quad \begin{array}{ccc} (-3) \times 7 & = & \underline{\underline{-21}} \\ \downarrow & & \downarrow \\ -ve & & +ve \end{array}$$

$$\textcircled{ii} \quad (-7) \times (-9) = 63$$

$$\textcircled{iii} \quad \underbrace{(-2) \times (-8)} \times (-3)$$
$$\Rightarrow \underline{16} \times (-3)$$
$$\Rightarrow \underline{\underline{-48}}$$

$$\underline{\underline{(-3) \times 7}} = -(3 \times 7)$$
$$= \underline{\underline{-21}}$$

$$\Rightarrow (-7) \times (-9) = +(7 \times 9)$$
$$= +63$$

\Rightarrow

$$\begin{array}{l} \text{(iv)} \quad \underbrace{(-1) \times (-2)} \times \underbrace{(-3) \times (-6)} \\ = 2 \times 18 \\ = \underline{\underline{36}} \end{array} \quad \left. \begin{array}{l} \Rightarrow 2 \times (-3) \times (-6) \\ \Rightarrow \underline{(-6)} \times \underline{(-6)} \\ \Rightarrow \underline{\underline{36}} \end{array} \right\}$$

$$\text{(v)} \quad (-3) \times (-5) \times (-2) = \boxed{-30}$$

Class 5

Division of Integers

(i) $+ve \div +ve = +ve$

for eg $15 \div 3 = 5$
↓ ↓ ↓
+ve +ve +ve

(ii) $-ve \div +ve = -ve$

for eg $\rightarrow (-15) \div 3 \Rightarrow -(15 \div 3) = -5$
↓ ↓ ↓
-ve +ve -ve

(iii) $+ve \div -ve = -ve$

for eg : $15 \div (-3) = -(15 \div 3) = -5$

(iv) $-ve \div -ve = +ve$

for eg : $(-15) \div (-3) = +(15 \div 3) = 5$
↓ ↓ ↓
-ve -ve +ve

$$\text{eg. } (-30) \div 6 = \frac{-30}{6} = -\left(\frac{30}{6}\right) = -5$$

$$\text{eg. } 140 \div (-7) = \frac{140}{-7} = -\left(\frac{140}{7}\right) = -20$$

Q. Evaluate $-3564 \div 22 = \underline{\underline{-\left(\frac{3564 \div 22}{}\right) = \underline{\underline{-162}}}}$

Absolute Value of an Integer



→ Actual numerical value of integer regardless of its sign (+ or -)

→ It is denoted by mod sign ||

⇒ Absolute value of an integer x , is denoted by $|x|$

eg.

$$\left. \begin{array}{l} |6| = 6 \\ | -7 | = 7 \end{array} \right\}$$

↑
read as mod (-7) or mod of (-7)

mod is abb. for modulus.

$$|-13| = \underline{\underline{13}}$$

↑

$$\text{mod } f \quad -13$$

$$|0| = \underline{\underline{0}}$$

$$|122| = \underline{\underline{122}}$$

Q. Find the product of $1296 \times (-74) = -(1296 \times 74)$
 $= \underline{\underline{-95904}}$

Q. Simplify : $4 \times 3 - 2 + 16 \div 8$
 $= \underline{\underline{12}} - \underline{\underline{2}} + \underline{\underline{2}}$
 $= 12$

BODMAS

↓

of

↓

multiplication

eg. $\left(\frac{1}{2}\right) \text{ of } (4) = \left(\frac{1}{2}\right) \times \left(\frac{4}{1}\right)$
 $= \frac{4}{2} = \underline{\underline{2}}$

Q. Simplify: $92 - [18 + 16 \div 4 \{26 - (14 - \overline{7-3})\}]$

$$= 92 - [18 + 16 \div 4 \{26 - (14 - 4)\}]$$

$$= 92 - [18 + 16 \div 4 \{26 - 10\}]$$

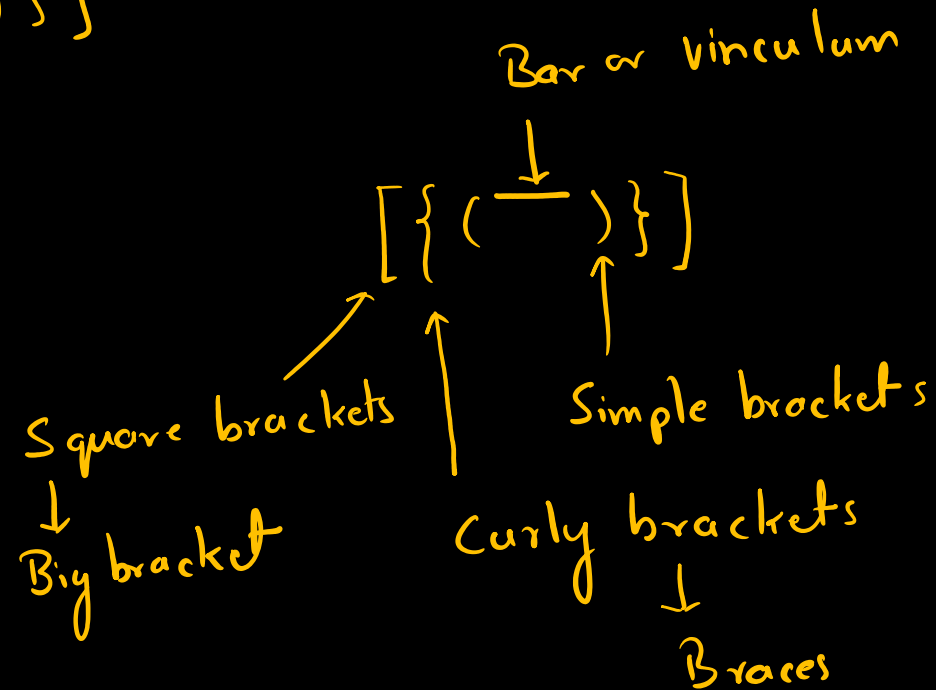
$$= 92 - [18 + 16 \div 4 \times 16]$$

$$= 92 - [18 + 4 \times 16]$$

$$= 92 - [18 + 64]$$

$$= 92 - 82$$

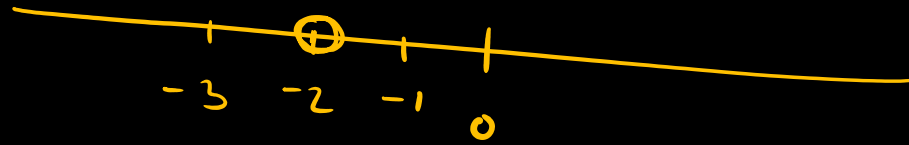
$$= \underline{\underline{10}}$$



Class 6

Gain \Rightarrow +ve value

Loss \Rightarrow -ve value



5000

$$\begin{array}{r} 5 \\ 144 \overline{) 15129.0} \\ \underline{-144} \\ 729 \\ \underline{-720} \\ 900 \\ \underline{864} \end{array}$$

$$\begin{aligned} & - \left(15129 \div 144 \right) \\ & - (105.06) \end{aligned}$$

Q. If P means multiplication, Q means division, R means addition and S means subtraction, then find the value of:

$$36P48Q16R15S23$$

$$\Rightarrow 36 \times 48 \div 16 + 15 - 23$$

$$\Rightarrow \underline{\underline{100}}$$

Q. Find the value of : $|-15| + |12|$

$$\Rightarrow 15 + 12$$

$$\Rightarrow \underline{\underline{27}}$$

Q. Arrange A, B & C in ascending order.

$$A: -12 + (-15)$$

$$B: -16 - (12)$$

$$C: -14 - (-12)$$

$$B < A < C$$

$$A = -12 + (-15) = -12 - 15 = -27$$

$$B = -16 - 12 = -28$$

$$C = -14 - (-12) = -14 + 12 = -2$$

Q. $| -5 | - | -3 |$

$\Rightarrow 5 - 3$

$\Rightarrow 2$

Q. P is neither positive nor negative, $Q = -|-9|$ and
R is the absolute value of -13 . Find the value of $P + Q + R$.

Sol.

| | | |
|------------------|--|-------------------------------|
| $P = 0$ | | $P + Q + R = 0 + (-9) + 13$ |
| $Q = - -9 = -9$ | | $= -9 + 13$ |
| $R = 13$ | | $= \underline{\underline{4}}$ |

Q. The cost of a pen is the largest two digit number (in \$).

The cost of a text book and a geometry box respectively are the successor and predecessor of the cost of pen.

Find the sum of the costs of the text book & geometry box (in \$)

$$\Rightarrow \text{Text book} = \$100$$

$$\text{geometry box} = \$98$$

$$\text{total cost} = \$ (100 + 98)$$

$$= \$198$$

Q. Simplify: $36 - 369 \div [-72 \div 24 \times 5 + 2(17 - \overline{7-18})]$

$$\Rightarrow 36 - 369 \div [-72 \div 24 \times 5 + 2(17 - (-11))]$$

$$\Rightarrow 36 - 369 \div [\underbrace{-72 \div 24} \times 5 + \underbrace{2(28)}]$$

$$\Rightarrow 36 - 369 \div [\underbrace{-3 \times 5} + 56]$$

$$\Rightarrow 36 - 369 \div [-15 + 56]$$

$$\Rightarrow 36 - 369 \div [41]$$

$$\Rightarrow 36 - 9$$

$$\Rightarrow \underline{\underline{27}}$$

Q. If A, B, C and D represents \times , \div , $+$ and $-$ respectively.
then find the value of 90B3A5D3C9

Ans \Rightarrow 156

Class 7

Doubt Clearing Class

$\Delta \rightarrow$ delta

+ \Rightarrow

- \Rightarrow

x \Rightarrow

\div \Rightarrow

Δ \Rightarrow

$$\begin{aligned} \text{(i)} \quad 2 \Delta 3 &= \underline{2 - 3 - (-2)} \quad \checkmark \\ \uparrow \quad \uparrow & \\ a \quad b & \\ &= -1 + 2 \\ &= \underline{1} \end{aligned}$$

$$\underline{\underline{a}} \Delta \underline{\underline{b}} = \underline{\underline{a - b - (-2)}} \quad \checkmark$$

$$\begin{aligned} \text{(ii)} \quad (-3) \Delta (-4) &= (-3) - (-4) - (-2) \\ \Downarrow \quad \Downarrow & \\ a \quad b & \\ &= -3 + 4 + 2 \\ &= -3 + 6 \\ &= \underline{\underline{3}} \end{aligned}$$

$$a = \textcircled{24} \rightarrow \textcircled{18}$$

$$b = \underline{(a-2)}$$

$$\boxed{a+b} = 24 + 22 \\ = 46$$

$$(a+b) = 18 + 16 \\ =$$

$$a = 18$$

$$\begin{array}{l} \underline{\underline{O}} \rightarrow \underline{a+b} \\ \underline{\underline{\Delta}} \rightarrow \underline{\underline{(a-b)}} \end{array}$$
$$\left. \begin{array}{l} a = 20 \\ b = 18 \end{array} \right\}$$

$$O = 20 + 18 = 38$$

$$\Delta = 2$$

$$\checkmark \underline{\underline{O + \Delta}} = 38 + 2 = \underline{\underline{40}}$$

$$\boxed{a \Delta b = a - b - (-2)}$$

$$\begin{array}{ccc} 2 & \Delta & 3 & = \\ \uparrow & & \uparrow & \\ a & & b & \end{array}$$

1, 2, 3, ...

$$\begin{array}{cccccccc}
 \underbrace{1-2}_{-1} & \underbrace{+3-4}_{-1} & \underbrace{+5-6}_{-1} & \underbrace{+7-8}_{-1} & \underbrace{+9-10}_{-1} & \underbrace{+11-12}_{-1} & \underbrace{+13-14}_{-1} & \underbrace{+15-16}_{-1} \\
 \downarrow & \downarrow & & & & & & \\
 (-1) & (-1) & (-1) & (-1) & (-1) & (-1) & (-1) & (-1) \\
 & & & & \downarrow & & & \\
 & & & & \boxed{-8} & & & \checkmark
 \end{array}$$

Method I

Method II:

$$\begin{array}{cccccccccccccccc}
 1 & -2 & +3 & -4 & +5 & -6 & +7 & -8 & +9 & -10 & +11 & -12 & +13 & -14 & +15 & -16 \\
 & & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\
 & & & & & & & & & & & & & & & &
 \end{array}$$

$$\begin{aligned}
 & \left(\underbrace{1+3+5+7+9+11+13+15} \right) + \left(\underbrace{-2-4-6-8-10-12-14-16} \right) \\
 & 64 + (-72) = \boxed{-8} \checkmark
 \end{aligned}$$

Calculate

$$(-5020 + 2320)$$

$$-709 - (-2700)$$

$$\begin{array}{cc} \downarrow & \downarrow \\ -2 & +5 \end{array}$$

$$\Rightarrow 3$$

$$\Rightarrow \begin{array}{c} \checkmark \\ -709 \\ \hline \end{array} + \begin{array}{c} \checkmark \\ 2700 \\ \hline \end{array}$$

$\Rightarrow 1991$

$$\begin{array}{r} 2700 \\ -709 \\ \hline \end{array}$$

Calculate the sum

$$2 + (-2) + 2 + (-2) + 2 + (-2) + \dots$$

(i) if the no. of terms is 140.

(ii) if the no. terms is 125.

$$\downarrow$$
$$\boxed{+2}$$

$$\underbrace{\underbrace{2 + (-2)}_0 + \underbrace{2 + (-2)}_0 + \underbrace{2 + (-2)}_0 + \dots}_{\downarrow 0} + \underbrace{+2 + (-2)}_0 + \underline{\underline{2}}$$

$$\Rightarrow \underline{\underline{0}}$$